

# MATHEMATICS FRAMEWORK

## for California Public Schools

Kindergarten Through Grade Twelve



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# APPENDIX B

## Works Cited

### Chapter 1

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