California Assessment of Student Performance and Progress

Grades 6 • 7 • 8

Teacher Guide to the Smarter Balanced Assessments

Mathematics

California Department of Education
Acknowledgments

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Introduction

The purpose of the Teacher Guide is to deepen teachers’ understanding of the Smarter Balanced Summative Assessments, their alignment with the California Common Core State Standards (CA CCSS), and their intended connection to classroom learning. The guide for mathematics is grade-span specific and synthesizes key information from a wide array of resources and resource sites, including:

- California Common Core State Standards
- *California Mathematics Framework for California Public Schools: Kindergarten through Grade Twelve (Mathematics Framework)*
- Content, item, task, and stimulus specifications
- Smarter Balanced Test Blueprints
- Smarter Balanced Practice Test Scoring Guides
- Smarter Balanced Communication Tools
- Smarter Balanced Digital Library

The mathematics guides are organized by grade span to highlight the changes in expectations as students move through the grade levels. Within the guides there are examples from Smarter Balanced Item Specifications that explain how student skills and knowledge are assessed and reported through collecting and scoring evidence. This grades three through five guide has an example from Claim 1, Concepts and Procedures, Grade Five. The grades six through eight guide shows a specification for Claim 3, Communicating Reasoning, Grade Eight, and the high school guide shows an example from Claim 4, Modeling and Data Analysis. The guide also provides examples of the range and types of items that appear on the assessments and the multiple resources that are available to teachers, students, and parents to “de-mystify” the assessments.

The Smarter Balanced Summative Assessments are part of the California Assessment of Student Performance and Progress (CAASPP) System.

The new Smarter Balanced Summative Assessments are different from the previous tests included in the Standardized Testing and Reporting (STAR) Program in several ways including:
• Designed to measure the expectations embodied in the CA CCSS adopted by the California State Board of Education in August 2010

• Emphasize deeper knowledge of core concepts and ideas within and across the disciplines along with analysis, synthesis, problem solving, communication, and critical thinking

• Include a greater variety of item types

• Capitalize on the strengths of computer adaptive testing (CAT), such as efficient and precise measurement across the full range of achievement

• Provide greater opportunities for classroom teachers to influence the design and operation of the assessment system
Section One: Purpose of the Guide—Resource for Planning Learning Events to Implement the Mathematics Framework for California Public Schools for Kindergarten through Grade Twelve Public Schools

These Teacher Guides are intended to be a resource for classroom teachers as they plan learning activities that fully implement the California Mathematics Framework using assessment feedback from the Smarter Balanced system of assessments.

Figure 1. Curriculum, Instruction, and Assessment Feedback Loop

Figure 1 shows the continuous feedback loop between curriculum, instruction, and assessment. Teachers use curriculum to plan instruction and use evidence from a variety of assessments to determine next steps in the teaching and learning cycle. The Mathematics Framework not only describes the state standards and research-based practices that support the standards, but connects overarching themes and the instructional shifts in the standards. Smarter Balanced assessment developers used similar overarching themes, instructional shifts, and understanding of the CA CCSS to build a fair and accurate assessment of the standards. They developed performance tasks and innovative items not seen before on large-scale state assessments to meet the demands of the key themes and the 21st century learning described below. The Mathematics Framework and Smarter Balanced assessments can function together to provide accurate and consistent evidence around the feedback loop.
Mathematics Framework for California Public Schools: Kindergarten Through Grade Twelve

The first stop for teachers in planning learning events is the Mathematics Framework. The guidance in this resource is research-based and includes practical examples to help all teachers.

Guiding Principles behind the development of the Mathematics Framework for California Public Schools: Kindergarten Through Grade Twelve (2015):¹

- Mathematical ideas should be explored in ways that stimulate curiosity, create enjoyment of mathematics, and develop depth of understanding.
- An effective mathematics program is based on a carefully designed set of content standards that are clear and specific, focused, and articulated over time as a coherent sequence.
- Technology is an essential tool that should be used strategically in mathematics education.
- All students should have a high-quality mathematics program that prepares them for college and careers.
- Assessment of student learning in mathematics should take many forms to inform instruction and learning.

Guiding Principle 1: Learning

Mathematical ideas should be explored in ways that stimulate curiosity, create enjoyment of mathematics, and develop depth of understanding.

For students to achieve mathematical understanding, instruction and learning must balance mathematical procedures and conceptual understanding. Students should be actively engaged in doing meaningful mathematics, discussing mathematical ideas, and applying mathematics in interesting, thought-provoking situations. Student understanding is further developed through ongoing reflection about cognitively demanding and worthwhile tasks.

Tasks should be designed to challenge students in multiple ways. Short- and long-term investigations that connect procedures and skills with conceptual understanding are integral components of an effective mathematics program. Activities should build upon students’ curiosity and prior knowledge and enable them to solve progressively deeper, broader, and more sophisticated problems.2

**Guiding Principle 2: Teaching**

An effective mathematics program is based on a carefully designed set of content standards that are clear and specific, focused, and articulated over time as a coherent sequence.

The sequence of topics and instruction should be based on what is known about how students’ mathematical knowledge, skill, and understanding develop over time. What and how students are taught should reflect not only the topics within mathematics but also the key ideas that determine how knowledge is organized and generated within mathematics.

Mathematical problem solving is the hallmark of an effective mathematics program. Skill in mathematical problem solving requires practice with a variety of mathematical problems as well as a firm grasp of mathematical techniques and their underlying principles. Armed with this deeper knowledge, students can use mathematics in flexible ways to attack various problems and devise different ways to solve any particular problem.

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2 Ibid. page 4
Mathematical problem solving calls for reflective thinking, persistence, learning from the ideas of others, and reviewing one’s own work with a critical eye. Students should be able to construct viable arguments and critique the reasoning of others. They should analyze situations and justify their conclusions, communicate their conclusions to others, and respond to the arguments of others.3

Guiding Principle 3: Technology

Technology is an essential tool that should be used strategically in mathematics education.

Technology enhances the mathematics curriculum in many ways. Tools such as measuring instruments, manipulatives (such as base-ten blocks and fraction pieces), scientific and graphing calculators, and computers with appropriate software, if properly used, contribute to a rich learning environment for investigating, exploring, developing, and applying mathematical concepts. Appropriate use of calculators is essential; calculators should not be used as a replacement for basic understanding and skills. Elementary students should learn how to perform the basic arithmetic operations independent of the use of a calculator (National Center for Education Statistics 1995). The use of a graphing calculator can help middle school and secondary students visualize properties of functions and their graphs. Graphing calculators should be used to enhance—not replace—student understanding and skills.

The Smarter Connection

Innovative items have been developed specifically for the Smarter Balanced assessments to engage students in real-world scenarios with multiple modes of response. All mathematics tools, including calculators, are embedded in the testing software. Test sections may be designed with “No Calculator” to conform to the Smarter Balanced calculator use policy that implements the intent of the Common Core State Standards.

Technology changes the mathematics to be learned, as well as when and how it is learned. For example, currently available technology provides a dynamic and exploration-driven approach to mathematical concepts such as functions, rates of change, geometry, and averages that was not possible in the past.4

3 Ibid. page 4
4 Ibid. page 5
Guiding Principle 4: Equity

All students should have a high-quality mathematics program that prepares them for college and careers.

The standards provide clear signposts along the way to the goal of college and career readiness for all students; they also accommodate a broad range of students, from those requiring a significant amount of extra support in mathematics to others needing minimal support or enrichment opportunities. To promote achievement of these standards, teachers should plan for, instruct, model, and support classroom discourse, reflection, use of multiple problem-solving strategies, and a positive disposition toward mathematics. They should have high expectations for all students. At every level of the education system, teachers should act on the belief that every child can and should learn challenging mathematics.

Because mathematics is the cornerstone of many disciplines, a comprehensive curriculum should include applications to everyday life and modeling activities that demonstrate the connections among disciplines. Schools should also provide opportunities for communicating with experts in applied fields to enhance students’ knowledge of these connections.5

Guiding Principle 5: Assessment

Assessment of student learning in mathematics should take many forms to inform instruction and learning.

A comprehensive assessment program is an integral component of an instructional program. It provides students with frequent feedback on their performance, teachers with diagnostic tools for gauging students’ depth of understanding of mathematical concepts and skills, parents with information about their children’s performance in the context of program goals, and administrators with a means for measuring student achievement.
Assessments take a variety of forms, require different amounts of time, and address various aspects of student learning. Gaps in knowledge and errors in reasoning can be identified when students “think aloud” or talk through their reasoning. By observing and questioning students as they work, teachers can gain insight into students’ abilities to apply appropriate mathematical concepts and skills, make conjectures, and draw conclusions.

Assessment should also be a major component of the learning process. As students help identify goals for lessons or investigations, they gain greater awareness of what they need to learn and how they will demonstrate that learning. Engaging students in this kind of goal setting can help them reflect on their work, understand the standards to which they are held accountable, and take ownership of their learning.6

### Learning in the 21st Century

In supporting 21st century learning, California is part of a growing national movement to teach students the problem-solving skills and critical thinking they need for college, careers, and civic life. The Partnership for 21st Century Skills (P21) developed a framework for 21st century learning comprising student outcomes and support systems. The student outcomes consist of the following elements:

- **Core subjects and 21st century interdisciplinary themes**, which include global awareness; financial, economic, business, and entrepreneurial literacy; civic literacy; health literacy; and environmental literacy
- **Life and career skills**, which include flexibility and adaptability, initiative and self-direction, social and cross-cultural skills, productivity and accountability, and leadership and responsibility

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6 Ibid. page 7
Learning and innovation skills, often referred to as the “4 Cs”: creativity and innovation, critical thinking and problem solving, communication, and collaboration.

Information, media, and technology skills, which include information literacy, media literacy, and ICT (information, communications, and technology) literacy.

Support systems provided by P21 include standards and assessments, curriculum and instruction, professional development, and learning environments.7

The Mathematics Framework guiding principles are important to keep in mind when planning learning activities. Daily opportunities to engage in rich learning using 21st century skills keep students engaged and develop students as partners in their own learning.

The Smarter Connection

Smarter Balanced performance assessment tasks were designed to meet the requirements of 21st century learning. The topics are real-world examples of issues that engage students. The performance tasks (PTs) are designed to elicit evidence of critical thinking, creative thinking, and consideration of the local and global impact of the issues.

7 Ibid. page 7
Section Two: Understanding and Using Smarter Balanced Test Design Principles to Support Classroom Learning Events

This section describes the evidence-centered design of the Smarter Balanced assessments and the hierarchical approach to item development. There are examples of how the test developers and teachers use evidence to accurately assess the learning required by the CA CCSS. Connecting the use of evidence-centered design and classroom learning activities allows a strong connection between Smarter Balanced results and resources.

Understanding the Fundamentals of Smarter Balanced Design

Knowing how the Smarter Balanced assessment system is developed, particularly how items are developed, can be helpful in understanding how to make the best use of the assessment resources and results. This knowledge should facilitate increasing the intentional connection between curriculum, instruction, and assessment.

The CA CCSS in Mathematics include content standards and standards for mathematical practice. In order to fully align the assessment to all of these standards, the Smarter Balanced test design has grade-level priority and supporting content clusters as assessment targets for Claim 1. For Claims 2, 3, and 4, the standards for mathematical practice emphasized at each claim and grade level are the assessment targets. (See the Mathematics Summative Assessment Blueprint on the Smarter Balanced Development and Design Web page at http://www.smarterbalanced.org/assessments/development/, under the Summative Test Blueprints tab, for grade-by-grade assessment targets in all claims.) The performance task in each grade uses priority content to frame a multi-step task and collect evidence on the student's ability to use content knowledge and mathematical practices effectively to solve the problems and communicate the rationale with supporting evidence.

The diagram and charts on the following pages describe the structure of Smarter Balanced item specifications—how evidence-centered design is used to develop items. A mathematics, grade eight example is used here from claim 1. While it is certainly not necessary to memorize this information, having a working knowledge of item development can facilitate use of results to enhance learning events. This item specification information is available for all Smarter Balanced assessments in resources listed at the end of this document.
Smarter Balanced has provided a zip file for each Claim and Grade of the item specifications used by test item writers to develop questions which can be found on the Smarter Balanced Development and Design Web page at http://www.smarterbalanced.org/assessments/development/ under the Item and Task Specification tab. You will be able to see exactly what instructions were given to clarify what was being tested and how to make sure there was tight alignment to the standards being assessed. The priority and supporting/additional domains and clusters tested in Claim 1 have statements describing *evidence required* to demonstrate deep understanding of the standards. In Claims 2, 3, and 4, the Standards for Mathematical Practice are being tested in the context of real-world problems. For these claims, the item specifications describe *expectations for students to provide evidence* of the ability to apply mathematical practices to solve problems.

When you open the link above, you will see a list of zip files. Choose the grade and claim you are interested in. For example, we have provided excerpts from Claim 3, Grade Eight specification here. Once you open the zip file, look for the assessment target. In our example in Figure 4 we are using assessment target B. We chose B because all students receive 3 questions covering targets B and E, including a question that may have a short text response. These questions are at DOK levels 3 and 4, the most rigorous levels of knowledge.

To illustrate the importance of evidence-centered design, Figure 3 displays the relationship among the overall claims, sub-domain assessment claims, assessment targets, and academic standards. This relationship is important, not only in the design and development of the Smarter Balanced items, but also in the interpretation and reporting of scores.

This claim/target/standard relationship is clearly articulated through the steps of the evidence-centered design model that Smarter Balanced assessments employ. The first step in the evidence-centered design approach is to define the content domains to be measured; in this case, the domains are English language arts/literacy and mathematics. The next step is to define the assessment claims that will be made about the domains. Claims are arguments derived from evidence about college and career readiness; Smarter Balanced claims are statements about what a student knows and is able to do. In the Smarter Balanced system, there are two kinds of claims: an “overall claim,” corresponding to performance on the entire assessment of English language arts/literacy or mathematics, and four domain-specific claims corresponding to performance in different areas in each of the assessments.
After carefully analyzing the CA CCSS and thinking about what students must know and be able to do in order to be prepared for college and career paths, Smarter Balanced identified four claims specific to English language arts and four claims specific to mathematics that focus on what students are expected to be able to do at each grade level.

Once the domains are defined and the claims are identified, the third step is to clearly identify the knowledge, skills, and abilities (KSAs) that form the content domain. In the Smarter Balanced system, the KSAs that are intended to be measured are called “assessment targets.” An assessment target defines the specific KSAs that students should be able to demonstrate within the domain. A large number of assessment targets are measured in the Smarter Balanced assessment system.

Once assessment targets are defined, the fourth step focuses on identifying the types of information that need to be collected from students to allow meaningful information to be gleaned about the student’s achievement of the assessment targets. The information Smarter Balanced elicits from students is considered to be evidence that can support or refute a claim about the student’s achievement of the assessment target.

Once the types of evidence to collect are determined, the final step focuses on developing items or tasks that will elicit the evidence regarding the knowledge, skills, and/or abilities that are articulated in the standards.
Figure 3a provides a content-specific example of the hierarchy of item development and illustrates how the domain overall claims, sub-domain assessment claims, assessment targets, and standards are connected, both in test development and reporting of scores. Recognizing the hierarchy makes the analysis of Smarter Balanced results easier to understand and emphasizes the importance of using the different levels of scores as contributors to a much larger picture.
Figure 3a. Anatomy of a Test—The Hierarchy of the Smarter Balanced Summative Assessment Example – Mathematics—Grade 8, Claim 3—Communicating Reasoning

<table>
<thead>
<tr>
<th>Overall Math Claim for Grade 8</th>
<th>Math Claim 3</th>
<th>Domain(s)</th>
<th>Estimated Number of Items Per Claim</th>
<th>Targets</th>
<th>Associated Standard(s) and Depth of Knowledge (DOK)(s)*</th>
</tr>
</thead>
<tbody>
<tr>
<td>Students can demonstrate progress toward college and career readiness in Mathematics</td>
<td>Students clearly and precisely construct viable arguments to support their own reasoning and to critique the reasoning of others.</td>
<td>EE, FA, GA, GB</td>
<td>8-10 items</td>
<td>are the bridge between the content standards and the assessment evidence that supports the claim; they ensure sufficiency of evidence to justify each claim</td>
<td></td>
</tr>
</tbody>
</table>

**Target B**

Construct, autonomously, chains of reasoning that will justify or refute propositions or conjectures. Tasks used to assess this target should ask students to develop a chain of reasoning to justify or refute a conjecture.

**Associated Standard(s) and Depth of Knowledge (DOK)(s)***

- 8.EE.A.1
- 8.EE.B.5
- 8.EE.B.6
- 8.EE.C.a
- 8.EE.C.b
- 8.EE.C.a
- 8.F.A.1
- 8.F.A.2
- 8.F.A.3
- 8.G.A.1
- 8.G.A.2
- 8.G.A.4
- 8.G.A.5
- 8.G.B.6
- 8.G.B.8
- DOK 3,4

* The Common Core State Standards require high-level cognitive demand. The Depth of Knowledge (DOK) refers to the cognitive rigor required of students to answer a question or perform a task. Four levels of DOK are considered in Smarter Balanced assessments, with each level requiring greater cognitive demand.

**Connecting the Smarter Balanced Mathematics Assessments to Classroom Learning**

By examining the item specifications for Communicating reasoning, Claim 3 (See Figure 4), teachers will be able to connect the evidence required in a Smarter Balanced assessment to learning goals and success criteria for a classroom learning event aligned to particular standards from mathematics Claim 1. The item specifications in Claim 1 detail the ways students will be tested on the deep understanding of the domains and clusters. The Development Notes of the Item Specifications describe appropriate approaches to using the same domain and cluster.
standards in problems to test the application of mathematical practices in Claims 2, 3, and 4. For a complete picture of an integrated approach to learning events with multiple entry points and opportunities for students to demonstrate evidence of deep understanding, cross-reference all of the grade level item specifications related to a domain and cluster in all of the Claims. (See Development Notes in Figure 4). The Smarter Balanced Item Specifications are a complex but necessary guiding resource as educators begin to analyze results. The specifications are a rich resource of information that includes the following:

- Intended claim (of what is being measured)
- Specific CA CCSS standards that are measured and connections to related standards in the grade below and the grade above
- Task models with example problems
- Types of items allowed
- Types of accommodations allowed
- Depth of knowledge, and
- Statements of evidence required of students

Often teachers want to know, “How good is good enough?” To give guidance to item writers, Smarter Balanced developed Range Achievement Level Descriptors (ALDs) for each grade, claim, and assessment target. These descriptions of what students should be able to do at each level of performance may guide the development of classroom rubrics and operationalize the expectations from the assessments. See the example in Figure 4:
**Claim 3:** Students clearly and precisely construct viable arguments to support their own reasoning and to critique the reasoning of others.

**Secondary Claim(s):** Items/tasks written primarily to assess Claim 3 will necessarily involve Claim 1 content targets. Related Claim 1 targets should be listed below the Claim 3 targets in the item form. If Claim 2 or Claim 4 targets are also directly related to the item/task, list those following the Claim 1 targets in order of prominence.

**Primary Content Domain:** Each item/task should be classified as having a primary, or dominant, content focus. The content should draw upon the knowledge and skills articulated in the progression of standards leading up to and including the targeted grade within and across domains.

**Secondary Content Domain(s):** While tasks developed to assess Claim 3 will have a primary content focus, components of these tasks will likely produce enough evidence for other content domains that a separate listing of these content domains needs to be included where appropriate. The standards in the NS domain in grades 6-8 can be used to construct higher difficulty items for the adaptive pool. The integration of the RP, EE, F, and G domains with NS allows for higher content limits within the grade level than might be allowed when staying within the primary content domain.

<table>
<thead>
<tr>
<th><strong>Target B:</strong></th>
<th>Construct, autonomously, chains of reasoning that will justify or refute propositions or conjectures.</th>
</tr>
</thead>
</table>

**Clarifications**

Tasks for Target B might include the types of examples called for in Target A as part of this reasoning, but should do so with a lesser degree of scaffolding than tasks that assess Target A alone. Some tasks for this target will ask students to formulate and justify a conjecture.

By “autonomous” we mean that the student responds to a single prompt, without further guidance within the task.

At the secondary level, these chains may take a successful student 10 minutes to construct and explain. Times will be somewhat shorter for younger students, but still giving them time to think and explain. For a minority of these tasks, subtasks may be constructed to facilitate entry and assess student progress towards expertise. Even for such “apprentice tasks,” part of the task will involve a chain of autonomous reasoning that takes at least 5 minutes.
<table>
<thead>
<tr>
<th>Standards</th>
<th>Expressions and Equations (EE)</th>
</tr>
</thead>
<tbody>
<tr>
<td>8.EE.A</td>
<td>Work with radicals and integer exponents</td>
</tr>
<tr>
<td>8.EE.A.1</td>
<td>Know and apply the properties of integer exponents to generate equivalent numerical expressions. <em>For example, 32 × 3–5 = 3–3 = 1/33 = 1/27.</em></td>
</tr>
<tr>
<td>8.EE.B</td>
<td>Understand the connections between proportional relationships, lines, and linear equations.</td>
</tr>
<tr>
<td>8.EE.B.5</td>
<td>Graph proportional relationships, interpreting the unit rate as the slope of the graph. Compare two different proportional relationships represented in different ways. <em>For example, compare a distance-time graph to a distance-time equation to determine which of two moving objects has greater speed.</em></td>
</tr>
<tr>
<td>8.EE.B.6</td>
<td>Use similar triangles to explain why the slope ( m ) is the same between any two distinct points on a non-vertical line in the coordinate plane; derive the equation ( y = mx ) for a line through the origin and the equation ( y = mx + b ) for a line intercepting the vertical axis at ( b ).</td>
</tr>
<tr>
<td>8.EE.C</td>
<td>Analyze and solve linear equations and pairs of simultaneous linear equations.</td>
</tr>
<tr>
<td>8.EE.C.7</td>
<td>Solve linear equations in one variable.</td>
</tr>
<tr>
<td>8.EE.C.8a</td>
<td>Understand that solutions to a system of two linear equations in two variables correspond to points of intersection of their graphs, because points of intersection satisfy both equations simultaneously.</td>
</tr>
<tr>
<td>Functions (F)</td>
<td></td>
</tr>
<tr>
<td>8.F.A</td>
<td>Define, evaluate, and compare functions.</td>
</tr>
<tr>
<td>8.F.A.1</td>
<td>Understand that a function is a rule that assigns to each input exactly one output. The graph of a function is the set of ordered pairs consisting of an input and the corresponding output.</td>
</tr>
<tr>
<td>8.F.A.2</td>
<td>Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions).</td>
</tr>
<tr>
<td><strong>8.F.A.3</strong></td>
<td>Interpret the equation ( y = mx + b ) as defining a linear function, whose graph is a straight line; give examples of functions that are not linear.</td>
</tr>
<tr>
<td><strong>Geometry (G)</strong></td>
<td></td>
</tr>
<tr>
<td><strong>8.G.A</strong></td>
<td>Understand congruence and similarity using physical models, transparencies, or geometry software.</td>
</tr>
<tr>
<td><strong>8.G.A.1</strong></td>
<td>Verify experimentally the properties of rotations, reflections, and translations:</td>
</tr>
<tr>
<td><strong>8.G.A.2</strong></td>
<td>Understand that a two-dimensional figure is congruent to another if the second can be obtained from the first by a sequence of rotations, reflections, and translations; given two congruent figures, describe a sequence that exhibits the congruence between them.</td>
</tr>
<tr>
<td><strong>8.G.A.4</strong></td>
<td>Understand that a two-dimensional figure is similar to another if the second can be obtained from the first by a sequence of rotations, reflections, translations, and dilations; given two similar two-dimensional figures, describe a sequence that exhibits the similarity between them.</td>
</tr>
<tr>
<td><strong>8.G.A.5</strong></td>
<td>Use informal arguments to establish facts about the angle sum and exterior angle of triangles, about the angles created when parallel lines are cut by a transversal, and the angle-angle criterion for similarity of triangles.</td>
</tr>
<tr>
<td><strong>8.G.B</strong></td>
<td>Understand and apply the Pythagorean Theorem.</td>
</tr>
<tr>
<td><strong>8.G.B.6</strong></td>
<td>Explain a proof of the Pythagorean Theorem and its converse.</td>
</tr>
<tr>
<td><strong>8.G.B.8</strong></td>
<td>Apply the Pythagorean Theorem to find the distance between two points in a coordinate system.</td>
</tr>
<tr>
<td><strong>Depth of Knowledge</strong></td>
<td>DOK 3,4</td>
</tr>
</tbody>
</table>
### Range Achievement Level Descriptors (ALD)

<table>
<thead>
<tr>
<th>Level</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Level 1</td>
<td>Students should be able to base arguments on concrete referents such as objects, drawings, diagrams, and actions and identify obvious flawed arguments in familiar contexts.</td>
</tr>
<tr>
<td>Level 2</td>
<td>Students should be able to find and identify the flaw in an argument by using examples or particular cases. Students should be able to break a familiar argument given in a highly scaffolded situation into cases to determine when the argument does or does not hold.</td>
</tr>
<tr>
<td>Level 3</td>
<td>Students should be able to use stated assumptions, definitions, and previously established results and examples to test and support their reasoning or to identify, explain, and repair the flaw in an argument. Students should be able to break an argument into cases to determine when the argument does or does not hold.</td>
</tr>
<tr>
<td>Level 4</td>
<td>Students should be able to use stated assumptions, definitions, and previously established results to support their reasoning or repair and explain the flaw in an argument. They should be able to construct a chain of logic to justify or refute a proposition or conjecture and to determine the conditions under which an argument does or does not apply.</td>
</tr>
</tbody>
</table>

### General Task Model Expectations for Target 3B

Items for this target should focus on the core mathematical work that students are doing around ratios and proportional relationships, the rational number system, and equations and expressions in grades six and seven and equations, functions, and geometry in grade eight with mathematical content from other domains playing a supporting role in setting up the reasoning contexts.

Items for this target can probe a key mathematical structure such as that found in expressions and equations, ratios and proportional relationships, and the rational number system.

Items for this target can require students to solve a multi-step, well-posed problem involving the application of mathematics to a real-world context. The difference between items for Claim 2A and Claim 3B is that the focus in 3B is on communicating the reasoning process in addition to getting the correct answer.

Note that in grades six through eight, items provide less structure than items for earlier grades to focus on justifying or refuting a proposition or conjecture. Many machine-scorable items for these task models can be adapted to increase the autonomy of student’s reasoning process but would require hand-scoring.

### Allowable Response Types

<table>
<thead>
<tr>
<th>Response Type</th>
</tr>
</thead>
<tbody>
<tr>
<td>Multiple-Choice, single correct response (MC); Multiple Choice, multiple correct response (MS); Equation/Numeric (EQ); Drag and Drop, Hot Spot, and Graphing (GI); Matching Tables (MA); Fill-in Table (TI) No more than six choices in MS and MA items.</td>
</tr>
</tbody>
</table>
## Allowable Stimulus Materials
Effort must be made to minimize the reading load in problem situations. Use tables, diagrams with labels, and other strategies to lessen reading load. Use simple subject-verb-object (SVO) sentences; use contexts that are familiar and relevant to all or most students at the targeted grade level. Target specific stimuli will be derived from the Claim 1 targets used in the problem situation.

## Construct-Relevant Vocabulary
Refer to the Claim 1 specifications to determine construct-relevant vocabulary associated with specific content standards.

## Allowable Tools
Any mathematical tools appropriate to the problem situation and the Claim 1 target(s). Some tools are identified in Standard for Mathematical Practice 5 and others can be found in the language of specific standards.

## Target-Specific Attributes
CAT items should take from 2 to 5 minutes to solve; Claim 3 items that are part of a performance task may take 3 to 10 minutes to solve.

## Accessibility Guidance
Item writers should consider the following Language and Visual Element/Design guidelines when developing items.

### Language Key Considerations:
- Use simple, clear, and easy-to-understand language needed to assess the construct or aid in the understanding of the context
- Avoid sentences with multiple clauses
- Use vocabulary that is at or below grade level
- Avoid ambiguous or obscure words, idioms, jargon, unusual names and references

### Visual Elements/Design Key Considerations:
- Include visual elements only if the graphic is needed to assess the construct or it aids in the understanding of the context
- Use the simplest graphic possible with the greatest degree of contrast, and include clear, concise labels where necessary
- Avoid crowding of details and graphics

Items are selected for a student’s test according to the blueprint, which selects items based on Claims and targets, not task models. As such, careful consideration is given to making sure fully accessible items are available to cover the content of every Claim and target, even if some item formats are not fully accessible using current technology.
Items and task assessing Claim 3 may involve application of more than one standard. The focus is on communicating reasoning rather than demonstrating mathematical concepts or simple applications of mathematical procedures.

Targeted content standards for Claim 3 should belong to the major work of the grade (reference table of standards shown below).

Claim 1 Specifications that cover the following standards should be used to help inform an item writer’s understanding of the difference between how these standards are measured in Claim 1 versus Claim 3. Development notes have been added to many of the Claim 1 specifications that call out specific topics that should be assessed under Claim 3.

Claim 3 items that require any degree of hand scoring must be written to primarily assess Target B.

At least 80% of the items written to Claim 3 should primarily assess the standards and clusters listed in the table that follows.

<table>
<thead>
<tr>
<th>6.RP.A</th>
<th>7.RP.A.2</th>
<th>8.EE.A.1</th>
</tr>
</thead>
<tbody>
<tr>
<td>6.RP.A.3</td>
<td>7.NS.A</td>
<td>8.EE.B.5</td>
</tr>
<tr>
<td>6.NS.A</td>
<td>7.NS.A.1</td>
<td>8.EE.B.6</td>
</tr>
<tr>
<td>6.NS.A.1</td>
<td>7.NS.A.2</td>
<td>8.EE.C.a</td>
</tr>
<tr>
<td>6.NS.C</td>
<td>7.EE.A.1</td>
<td>8.EE.C.b</td>
</tr>
<tr>
<td>6.NS.C.5</td>
<td>7.EE.A.2</td>
<td>8.EE.C.a</td>
</tr>
<tr>
<td>6.NS.C.6</td>
<td></td>
<td>8.F.A.1</td>
</tr>
<tr>
<td>6.NS.C.7</td>
<td></td>
<td>8.F.A.2</td>
</tr>
<tr>
<td>6.EE.A</td>
<td></td>
<td>8.F.A.3</td>
</tr>
<tr>
<td>6.EE.A.3</td>
<td></td>
<td>8.G.A.1</td>
</tr>
<tr>
<td>6.EE.A.4</td>
<td></td>
<td>8.G.A.2</td>
</tr>
<tr>
<td>6.EE.B</td>
<td></td>
<td>8.G.A.4</td>
</tr>
<tr>
<td>6.EE.B.6</td>
<td></td>
<td>8.G.A.5</td>
</tr>
<tr>
<td>6.EE.C.9</td>
<td></td>
<td>8.G.B.6</td>
</tr>
<tr>
<td></td>
<td></td>
<td>8.G.B.8</td>
</tr>
</tbody>
</table>
The Smarter Balanced assessments are designed to gather evidence from students that shows what they know about the standards. To keep the assessment consistent with the standards and classroom learning, teachers were actively engaged in the review and revision of the evidence statements to accurately describe what performance would meet the standard at a particular grade level. For the purposes of the assessments, the standards are organized into assessment target groups. As illustrated in Figure 3, the assessment targets provide a bridge between the content standards and the evidence that supports the claims.

The Smarter Balanced evidence statements aligned to domain and cluster standards are provided in the Smarter Balanced Item Specifications for Claim 1, Concepts and Procedures. For an example of a Claim 1 Item Specifications with evidence statements, see this grades three through five teacher guide, Figure 4 or all Claim 1 Item Specifications. In the grades six through eight teacher guide, Figure 4 provides an example of a grade eight mathematics item specification. In that example, there is a description of the expectations for students using mathematical practices in the context of problems using content knowledge of the priority standards as articulated in the Development Notes. In the high school guide, there is an example of item specifications for Claim 4, Modeling and Data Analysis in Figure 4.

Figure 5 describes how the Smarter Balanced expectations statements may be used in conjunction with classroom evidence to maximize opportunities for demonstrations of student learning in applying mathematical practices.

Figure 6 graphically displays the use of the Item Specifications in helping craft a classroom learning event consistent with the Smarter Balanced expectations statements in Claim 3 specifications.
Step 1: Match the Standards for Mathematical Practice with the Claim and corresponding Target on the Task Model.

**Standard of Mathematical Practice 3:** Construct viable arguments and critique the reasoning of others.

**Grade 8, Claim 3: Communicating Reasoning:** Target B. Construct, autonomously, chains of reasoning that will justify or refute propositions or conjectures.


**Expectations Rubric:**

(2 points) The student includes the correct numeric value in the response (80) and provides a coherent, complete explanation or sequence of computations that shows where this comes from (see Examples).

(1 point) The student enters the correct numeric value but does not provide a coherent explanation OR the student provides an incorrect speed and includes an explanation that shows an understanding of how the answer could be found, but with some computational errors or a small misstep in reasoning.

Step 3: Become familiar with the task models and example questions used in developing the items so that students also gain familiarity with the vocabulary and phrasing of these task models before the test.

Primary Target 3B (Content Domain RP), Secondary Target 1A (CCSS 7.RP.A), Tertiary Target 4F (Note: The content standard is from grade seven)

A car is traveling at a constant speed and drove 75 miles in 1.5 hours. One mile is approximately 1.6 kilometers. Approximately how fast is the car traveling in kilometers per hour?

Explain or show clear steps for how you determined your answer.

**Example 1**

Going 75 miles in 1.5 hours is the same as going 50 miles per hour.

50 miles is $50 \times 1.6 = 80$ km.

A car driving 50 miles per hour is driving 80 kilometers per hour.

**Example 2**

75 miles in 1.5 hours is $75/1.5 = 50$ mi/hr.

$50$ mi/hr $\times 1.6$ km/mi $= 80$ km/hr.

The car is traveling at 80 kilometers per hour.

**Response Type:** Short Text (hand scored)
Figure 6: How to Use the Item Specifications and Evidence Statements to Design a Lesson or Activity

**Curriculum**

**Teachers and Students...**
- Collaborate on Learning Goals
- Identify Success Criteria
- Collect Evidence of Mastery Similar to the Evidence Required on the Tests

**Math Domains and Clusters**
- Match Domains and Clusters to Claims and Targets
- Find Evidence Statements from Test Item Specifications

**Students...**
- Practice Tasks that require Deep Understanding
- Show Applications of Their Learning in New Situations
Section Three: Instruction with Planned Evidence Collection and Feedback Helps Teachers and Students Improve Student Learning

How can teachers use the Smarter Balanced Tools to enhance the teaching and learning experience?

One of the many challenges for teachers in planning effective learning events for students is to know the specific needs of each student. Planned evidence collection during daily instruction using the formative assessment process, after a unit of instruction on a key topic using interim assessments, and at the end of the year with summative assessments provides a balanced view of the student’s learning progress. The summative assessments can affirm the evidence collected from other sources in the classroom during the school year.

The Mathematics Framework emphasizes the integrated nature of mathematics domains and clusters. No standard should be taught in isolation. Students respond to high quality, real-world tasks that apply content knowledge using standards of mathematical practice.

Performance assessment tasks based on the Smarter Balanced model give students the opportunity to demonstrate a deep understanding of the problem-solving process, using modeling and data analysis, and communicating reasoning. Teachers and students can build evidence for a solution using real-world source materials and engaging, age-appropriate questions. Examples of student responses to performance tasks on the Practice Tests as well as the Range ALD descriptions are resources for teachers and students to use to develop classroom rubrics to guide the evaluation of classroom learning.

Assessment for Learning

The exemplar assessment reflects the classroom learning environment and experience of the student and collects evidence that can be interpreted to evaluate the student’s level of understanding of the standard being assessed. This is true for classroom
assessment as well as large-scale statewide assessment. The *Mathematics Framework* distinguishes between assessment for learning and assessment of learning. An annual **summative** assessment, like the Smarter Balanced Summative Assessment, is an assessment of learning; while it does not provide teachers with immediate, actionable feedback on student learning, it can provide educators with valuable information to enhance the teaching and learning process, as well as provide a valid and reliable measure of achievement at the student, school, district, and state levels.

In contrast, assessment for learning, or **formative** assessment, occurs during instruction, allowing teachers to adapt instruction as needed. Teaching with the formative assessment process includes challenging students with rigorous tasks. Lessons with formative assessments clarify the student learning goals and success criteria and elicit evidence of student understanding. As teachers interpret this evidence, instruction may be adjusted to optimize learning. Learning is accomplished when students demonstrate and apply the knowledge and skills of the standards. Students take an active role in their learning by using rubrics for self-assessment and peer assessment. Students collaborate with teachers to plan next steps to move up the learning progression and apply what they know to new situations to solve real-world problems. Using the formative assessment process, in conjunction with the Smarter Balanced resources, tools and results can maximize the use of assessments and assessment data in the teaching and learning cycle. Below are additional Smarter Balanced resources that can support and enhance teaching and learning.

The Smarter Balanced Assessment System offers a suite of tools and resources that support classroom-based formative assessment practices. These tools are located on the Smarter Balanced Digital Library Web page at [http://www.cde.ca.gov/ta/tg/sa/diglib.asp](http://www.cde.ca.gov/ta/tg/sa/diglib.asp). The Digital Library has been built by and for educators within the Smarter Balanced Consortium. (All subscribers must provide a user name and password in order to log on to the Digital Library.)

**Steps Toward Creating a More Authentic Assessment**

Teachers from Smarter Balanced states, including California, participated in all phases of the test development process to push toward the delivery of an authentic assessment in a statewide system.

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As part of the test development process, Smarter Balanced held cognitive labs in participating states (including California). Students were asked to talk about what they were thinking when they answered trial test questions. This way, test developers could determine if the students were actually thinking about what the question writers intended when students answered the question. Using results from the cognitive labs, the student responses confirmed that the sample questions were at the correct level of rigor and deep understanding of the standard being tested. The labs also validated the usefulness of the technology tools for students with special needs, the ability of early elementary students to use the keyboard to manipulate the technology tools, and other critical concerns addressed by the computer-based delivery of the test.

Teachers are able to make use of the Smarter Balanced CAT items and performance tasks presented on the Practice Test to see how the collection of evidence from each question adds evidence to support all the claims in an integrated and coherent approach. These Practice Tests may be used in a whole group setting, or even used as starting points for creating classroom items or performance tasks. Teachers can gain an understanding of how the combination of evidence adds to the overall evaluation of student understanding of the math domains and clusters as a whole. With this understanding, teachers may construct their own classroom models for collecting evidence that align pieces of evidence to each standard being assessed.

**The Smarter Connection**

Figure 7 provides a side-by-side comparison between the Major Principles of the California Common Core State Standards in Mathematics and the elements of the Smarter Balanced test design that support these shifts.
### Figure 7. Side by Side Comparison of the Major Principles of the California Common Core State Standards in Mathematics and Smarter Balanced Test Design

<table>
<thead>
<tr>
<th>California Common Core State Standards in Mathematics</th>
<th>Smarter Balanced Test Design</th>
</tr>
</thead>
<tbody>
<tr>
<td>Focus</td>
<td>Focus</td>
</tr>
<tr>
<td>Place strong emphasis where the standards focus</td>
<td>There are grade-level specific blueprints that detail the priority clusters and the additional and supporting clusters in Concepts and Procedures (Claim 1) which comprise 50% of the assessment. Each cluster is assigned a number of questions consistent with the grade level focus. Performance assessment tasks are developed using designated priority standards at each grade level.</td>
</tr>
<tr>
<td>Coherence</td>
<td>Coherence</td>
</tr>
<tr>
<td>Think across grades, and link to major topics in each grade</td>
<td>The item specifications link the related standards from the grade below, grade at, and grade above to show the coherence of the content across grades.</td>
</tr>
<tr>
<td>Rigor</td>
<td>Rigor</td>
</tr>
<tr>
<td>In major topics, pursue with equal intensity:</td>
<td>Key aspects of the grade level focus standards are tested in Claims 2, 3, and 4 to demonstrate student understanding of the application of knowledge, problem-solving, and mathematical practices. The targets in Claims 2, 3, and 4 are Standards for Mathematical Practice.</td>
</tr>
<tr>
<td>- Conceptual understanding</td>
<td></td>
</tr>
<tr>
<td>- Procedural skill and fluency</td>
<td></td>
</tr>
<tr>
<td>- Application</td>
<td></td>
</tr>
</tbody>
</table>


Item and Task Types Collect Evidence in New Ways

The Smarter Connection

The new Smarter Balanced Summative Assessments elicit greater, more precise evidence of a student’s knowledge, reasoning, and understanding.

California’s previous state tests relied almost exclusively on multiple-choice questions, which are easy to score, but somewhat limited in their ability to assess higher-order thinking skills.

Item types and tasks include, but are not limited to:

- Multi-part questions that require students to use evidence from text
- Constructed-response items, which address skills of greater complexity and require students to demonstrate their thinking
- Technology-enhanced items, which require students to manipulate information
- A performance task (PT), which is an extended activity that measures students’ ability to integrate knowledge and skills across multiple standards

Recommended Resource

All teachers are strongly encouraged to take the Practice Test to become familiar with the types of questions that students will be given on the Smarter Balanced Assessments. The Practice Test is posted on the CAASPP Web Portal at http://www.caaspp.org/practice-and-training/index.html.

Accessibility Supports and Accommodations Help All Students Meaningfully Participate

The computer-adaptive Smarter Balanced Summative Assessments provide all students with greater flexibility than do traditional pencil-and-paper tests. For example, students can increase the size of an image by using the “Zoom In” option or can highlight key words as they read a passage. Additional options are available to students with special needs. The online tools and supports make the assessments accessible to students and ensure that the test results provide a fair and accurate measure of their achievement.

The Smarter Connection

The wide array of Smarter Balanced accessibility supports and accommodations make the tests more user friendly and allow students to better demonstrate what they know and are able to do in mathematics.
Three major types of supports and accommodations that are available on the Smarter Balanced Summative Assessments are as follows:

- Universal tools, such as highlighting, digital notepads, zooming in/out, embedded glossary, writing tools for the ELA full writes, and calculators for some mathematics items—available to all students

- Designated supports, such as color contrast or masking, as well as bilingual glossaries and translated test directions—available to any student who has been identified with a special need, as determined by an educator or support team

- Accommodations, such as text-to-speech, closed captioning and on-screen American Sign Language translation—available to students with an individualized education plan (IEP) or Section 504 plan

Recommended Resource

For more information, please see the CDE CAASPP Student Accessibility Supports Web page at http://www.cde.ca.gov/ta/tg/ca/accesssupport.asp.
Section Four: Using Smarter Balanced Score Reports to Analyze Data and Improve Learning

The third step in the feedback loop is to analyze the student data trends to evaluate the learning that has occurred by the students. Teachers compare the curriculum intended for learning by students with the curriculum actually learned as evidenced by the results on multiple measures, including the Smarter Balanced assessments. Teachers look at multiple sources of data, including individual results and class data to understand the “big picture” of student learning.

For Smarter Balanced results, each student’s score is placed on a continuous scale that is able to show growth from year to year. With class-level data, teachers may identify strengths and gaps of understanding in the content areas which can lead to adjustments in the teaching and learning cycle.

The Smarter Balanced assessments are designed to assess student learning at a point in time, using technology to eliminate accessibility barriers and maximize the opportunity for students to show what they know. The computer adaptive software is a critical design aspect allowing students to answer questions at an appropriate level of difficulty to collect positive evidence of knowledge that leads to an accurate score for each student.

The Smarter Connection

What do the results on the Smarter Balanced Assessments (summative and interim) indicate about student strengths and needs?

Computer Adaptive Testing: Appropriate Assessment for Each Student

In computer adaptive testing (CAT), the computer program adjusts the difficulty of questions on the basis of student responses. For example, a student who answers a question correctly will receive a subsequent question that is more challenging, while an incorrect answer will generate a less challenging question. This approach represents a significant improvement over traditional paper-and-pencil assessments, in which all students receive the same test items, and provides teachers and schools with a more accurate way to evaluate student achievement and measure growth over time.
Practice Tests and Training Tests Available for Teachers, Students, and Parents

Teachers are able to use sample student responses and the Smarter Balanced Practice Test Scoring Guides to find comparisons to student work in their own classes or from students within the grade span. Once teachers recognize the difficulty and quality of “at standard” and “above standard” responses, they are able to plan learning progressions for students to help them move from “where they are” to “where they need to be” to improve their performance.

Note: It is important that all students gain familiarity with the keyboard and are able to type text of short-to-medium length (for constructed-response items) as well as a full-length essay (for the ELA PT).

Recommended Resource
For more information, see the Smarter Balanced Web page at http://www.smarterbalanced.org/assessments/practice-and-training-tests/.

How Student Performance Is Reported on the Smarter Balanced Assessments

Recall how the Smarter Balance Summative Assessment scores are provided in different grain sizes—that is, different scores provide varying levels of detail that, taken together, can offer a productive way to examine scores. The Smarter Balanced Summative Assessment is intended to be an accurate measure of student performance at a point in time that is aligned to the state standards. Overall performance on mathematics is reported for students and for subgroups of students and provides a general description of achievement. These overall scores are particularly useful in an accountability system and can be helpful in developing the Local Control Accountability Plans required of all California districts. Claim performance may be used to help teachers understand student’s strengths and needs as well as the strengths of groups, e.g., grades programs, subgroups. The following is an explanation of the overall mathematics score and each content claim score.

Recommended Resource
Overall Score and Achievement Level—
Shows Student Performance on the Difficulty Scale

Students receive an overall scale score for Mathematics. On the mathematics assessment, Claim 1, Concepts and Procedures, is 50% of the overall score; Claims 2 and 4, Problem-solving, Modeling, and Data Analysis, are reported together for 25% of the score; and Claim 3, Communicating Reasoning is the remaining 25% of the overall score. The score falls along a continuous vertical scale (from approximately 2,000 to 3,000) that increases across grade levels. Based on this score, a student is determined to be at one of four achievement levels.

Let's consider the Mathematics scale score range for grade eight, which spans over five hundred points:

$$2,265 \quad \leftrightarrow \quad 2,802$$

Within that range, there are four distinct achievement levels, as shown in Figure 10:

**Figure 10. Grade Eight Mathematics Scale Scores and Achievement Levels**

<table>
<thead>
<tr>
<th>Standard Not Met</th>
<th>Standard Nearly Met</th>
<th>Standard Met</th>
<th>Standard Exceeded</th>
</tr>
</thead>
<tbody>
<tr>
<td>2265–2503</td>
<td>2504–2585</td>
<td>2586–2652</td>
<td>2653–2802</td>
</tr>
</tbody>
</table>

The achievement levels take into account the level of difficulty of the test questions. Because the test is computer adaptive, students who consistently answer correctly will be steered toward items at the higher end of the continuum, allowing for the opportunity to achieve at the Standard Exceeded level. Those who consistently answer incorrectly will be steered toward the lower end, possibly resulting in the Standard Not Met level. Regardless of the level, the score provides an accurate reflection of performance against a set of academic standards and performance expectations.

For example, teachers may look at grade-level

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**The Smarter Connection**

The Smarter Balanced Summative Assessment results help teachers develop lines of inquiry to improve the curriculum, enhance the teaching and learning cycle, and make learning more meaningful to students.
data to observe the trends of students toward each end of the difficulty continuum. If groups of students, on average, have met or exceeded the standards, there is evidence that the classroom learning events helped students practice applying deep understandings of the standards. If groups of students, on average, have not met or nearly met the standards, then teachers may consider the types of learning events, practice, and opportunities available for students to apply those deep understandings.

The tables for Smarter Balanced scale score ranges, which include the scale score ranges for ELA and mathematics by content area, grade level, and achievement level, are posted on the Smarter Balanced Scale Score Ranges web page at https://www.smarterbalanced.org/assessments/development/percentiles/.

Claim Level Achievement—Shows General Student Performance in Content Areas

The test reports will also highlight a student’s performance on each claim for Mathematics. A claim is a broad statement that identifies the set of knowledge and skills to be measured on the assessment. Figure 8 identifies the claims for Mathematics.

**Figure 8. Mathematics Claim Areas**

<table>
<thead>
<tr>
<th>Mathematics Areas (Claims)</th>
<th>For Grades Three, Four, and Five</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\frac{a}{b} = c$</td>
<td>Concepts &amp; Procedures</td>
</tr>
<tr>
<td></td>
<td>Applying mathematical concepts and procedures</td>
</tr>
<tr>
<td></td>
<td>Problem Solving &amp; Modeling/Data Analysis</td>
</tr>
<tr>
<td></td>
<td>Using appropriate tools and strategies to solve real world and mathematical problems</td>
</tr>
<tr>
<td></td>
<td>Communicating Reasoning</td>
</tr>
<tr>
<td></td>
<td>Demonstrating ability to support mathematical conclusions</td>
</tr>
</tbody>
</table>

Student performance for each claim is reported as “Above Standard,” “Near Standard,” or “Below Standard.” These are designed to be general indicators of the strengths or needs of the student or a group.

Recommended Resource

Sample score reports for other grade levels are available on the CDE’s CAASPP Student Score Report Information Web page at http://www.cde.ca.gov/ta/tg/ca/caasppssrinfo.asp.
of students in each claim area. The number of items making up the claim performance varies based on the specifications of the test blueprint so caution must be used in the interpretations of these scores. It is recommended that other evidence be considered along with the claim score as decisions are made about curriculum and instruction.

Use Group-Level Data to Identify Trends in Curriculum Strengths and Gaps

At the end of the school year it is time to take stock of the successes in student learning. The tight alignment of the Smarter Balanced assessments to the Mathematics Framework makes the assessment results a valuable resource to begin an inquiry, a thoughtful deliberate discussion about how we can maximize the appropriate use of these results. The questions on page 36 can help guide a discussion of what the results show about student and group performance and the implications for building on student strengths and meeting student needs with curriculum resources.

Assessment Target Reports

Assessment Target Reports are a new resource for administrators and teachers. These reports show the relative performance of groups of students on assessment targets within a Concepts and Procedures, Claim 1, as long as there are sufficient responses (at least 10) for a particular target. The reports show how a group of students performed on a target compared to the overall performance on the test, which includes the performance on the other claims on the CAT and the performance assessment task. Mathematics is intended to be learned as an integrated content area. Using the formative assessment process, specific evidence for each target may be collected in multiple parts of an integrated task. By reflecting on students' time-on-task and their opportunities for mastery throughout the year in each target area, teachers are able to compare the intended learning of groups of students with the evidence of learning on the Smarter Balanced assessments.

Assessment target score reports should serve as a starting point in an overall investigation of students' strengths and weaknesses and constitute only one of many sources of evidence that should be used in evaluating student performance. Assessment target scores based on fewer than 50 students may be less reliable and will have fewer unique items contributing to the overall target summary. Target score reports are not appropriate for individual students.
The following chart lists the icons used to show the relative performance of students on the target versus the whole test.

<table>
<thead>
<tr>
<th>Icon</th>
<th>Target Level</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>+</td>
<td>Better than Performance on the test as a whole</td>
<td>This target is a relative strength. The group of students performed better on items from this target than they did on the rest of the test as a whole.</td>
</tr>
<tr>
<td></td>
<td>Similar to performance on the test as a whole</td>
<td>This target is neither a relative strength nor a relative weakness. The group of students performed about as well on items from this target as they did on the rest of the test as a whole.</td>
</tr>
<tr>
<td>−</td>
<td>Worse than performance on the test as a whole</td>
<td>This target is a relative weakness. The group of students did not perform as well on items from this target as they did on the rest of the test as a whole.</td>
</tr>
<tr>
<td></td>
<td>Insufficient Information</td>
<td>Not enough information is available to determine whether this target is a relative strength or weakness.</td>
</tr>
</tbody>
</table>

The Assessment Target Report is generated for groups of students and is not available for individual students. Assessment targets for which there are at least 10 items available in the Smarter Balanced item pool are included on the Assessment Target Report.

These Assessment Target Reports may help validate other evidence of deep understanding collected during classroom instruction. A data-inquiry process using this target group-level data can be helpful at the classroom level, grade level, school level and districtwide to understand the successes and needs of students. Remember that these target results are relative to the total test score; therefore, recognizing the overall achievement level will be important in considering instructional strategies that address strengths or weaknesses.
Guiding Questions to Analyze Group-Level Data

- What is the trend for this group of students related to being “on track” for college readiness? (Overall scores)

- What is the range of overall performance for my class or other groups of students? (Overall scores)

- Which claims appear to be areas of strength for my students? (Claim Achievement Levels)

- Which claims might be areas of need? (Claim Achievement Levels)

- Which targets show a variance from the whole test performance? (Assessment Target Report)

- Which curriculum resources might help me address student needs for the coming year? (Curriculum Resources)

- How do I find examples of student work that meet the goals for being “on track” for college readiness? (Practice Test Scoring Guides)

- What evidence do I need during classroom instruction to know that my students are making progress toward meeting the learning goals for each claim? (Evidence Statements from Item Specifications)

- Where might I find examples of evidence to meet the learning expectations for each claim? (Item Specifications and Practice Test Scoring Guides)

- How can I help my students gain familiarity with the types of questions that they will encounter on the Smarter Balanced Summative Assessments? (Item Specifications: See Appropriate Stems for Writing Items for a Target, Practice Test)

- How might I use the Smarter Balanced resources (Item Specifications, Achievement Level Descriptors, etc.) to increase my students’ awareness of performance expectations?

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Section Five: Conclusion—Putting It All Together

As teachers build their understanding of the intent of the standards and the relative quality of the evidence of student understanding, they increase their capacity to make adjustments in daily classroom learning events to help students move forward to meet and exceed expectations.

The Smarter Connection
Teachers can have confidence in the reliability of the information from the Smarter Balanced assessments because of the tight alignment of the assessments to the Mathematics Framework and the customization of each student’s test to get the best evidence from each student for the most accurate score.

Smarter Balanced Resources for Teachers from the Smarter Balanced Digital Library

Smarter Balanced is an assessment system designed to support teachers and students in learning. The assessment resources complement the content standards and the instructional guidance that is provided in the Mathematics Framework. The Smarter Balanced test development resources, practice test scoring guides, and the different kinds of achievement level descriptors illustrate the thinking behind the assessment questions and the rationale for correct answers. The Smarter Balanced Digital Library has resources crafted by teachers, for teachers to share within the Smarter Balanced community. Below are examples of what is contained in the Digital Library.

- Assessment Literacy Module: Understanding the Learner
  https://www.smarterbalancedlibrary.org/content/understanding-learner

- Assessment Literacy Module: Students as Partners in Their Own Learning—Grades 6–12
  https://www.smarterbalancedlibrary.org/content/students-partners-their-own-learning-grades-6-12

- Illustrative Mathematics RP Module
  https://www.smarterbalancedlibrary.org/content/illustrative-mathematics-rp-module

- Proportional Reasoning: CBAL (TM) Activity Set, Handbook and Teacher Videos

12 To access the links for these resources, the user must be logged into the Smarter Balanced Digital Library.
Formative Assessment Process

Teaching includes the formative assessment process with rigorous tasks. Lessons with formative assessments clarify the student learning goals and success criteria and elicit evidence of student understanding. As teachers interpret this evidence, instruction may be adjusted to optimize learning. Learning is accomplished when students demonstrate and apply the knowledge and skills of the standards. Students take an active role in their learning by using rubrics for self-assessment and peer assessment. Students collaborate with teachers to plan next steps to move up the learning progression and apply what they know to new situations to solve real-world problems.

Using the formative assessment process in conjunction with the Smarter Balanced resources, tools, and results, can maximize the use of assessments and assessment data in the teaching and learning cycle.

Below are additional Smarter Balanced resources that can support and enhance teaching and learning.

Digital Library
- Assessment Literacy Module: Understanding the Formative Assessment Process
  [https://www.smarterbalancedlibrary.org/content/understanding-formative-assessment-process](https://www.smarterbalancedlibrary.org/content/understanding-formative-assessment-process)

Smarter Balanced Web Site
- Smarter Balanced Assessment Consortium: Signing Guidelines

- Smarter Balanced Assessment Consortium: Tactile Accessibility Guidelines

- Smarter Balanced Assessment Consortium: Bias and Sensitivity Guidelines
WestEd Web Site

- Understanding Proficiency
  Located on the WestEd Understanding Proficiency Web page at http://understandingproficiency.wested.org

- Raising the Bar on Instruction
  Located on the WestEd Research-based tools, resources, and services Web page at http://raisingthebar.wested.org

California Assessment of Student Performance and Progress (CAASPP)

- Information about the CAASPP System of assessments is available at http://www.cde.ca.gov/ta/tg/ca/


- The Digital Library Professional Development Series is available at http://www.cde.ca.gov/ta/tg/sa/instructlearning.asp